

Universal spin dynamics in two-dimensional Fermi gases

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Harnessing spins as carriers for information has emerged as an elegant extension to the transport of electrical charges¹. The coherence of such spin transport in spintronic circuits is determined by the lifetime of spin excitations and by spin diffusion. Fermionic quantum gases are a unique system to study the fundamentals of spin transport from first principles since interactions can be precisely tailored and the dynamics is on time scales which are directly observable^{2–11}. In particular at unitarity, spin transport is dictated by diffusion and is expected to reach a universal, quantum-limited diffusivity on the order of \hbar/m . Here, we study the non-equilibrium dynamics of a two-dimensional Fermi gas following a quench into a metastable, transversely polarized spin state. Using the spin-echo technique¹², we measure the yet lowest transverse spin diffusion constant^{13,14} of $0.25(3) \hbar/m$. For weak interactions, we observe a coherent collective transverse spin-wave mode that exhibits mode softening when approaching the hydrodynamic regime.

Studying transport in low-dimensional nanostructures has a long and rich history because of its non-trivial features and its relevance for electronic devices. The most common case, charge transport, has great technological implications and it determines the current-voltage characteristics of a device. With the development of the field of spintronics¹, however, also spin transport has moved into the focus of the research interest. Spin transport has unique properties, setting it aside from charge transport: Firstly, the transport of spin polarization is not protected by momentum conservation and is greatly affected by scattering^{5,15}. Therefore, the question arises what is the limiting case of the spin transport coefficients when interactions reach the maximum value allowed by quantum mechanics? Secondly, unlike charge currents (which lead to charge separation and the buildup of an electrical field, counteracting the current), spin accumulation does not induce a counteracting force.

The main mechanism to even out a non-equilibrium magnetization $\vec{M}(\vec{r}, t) = M(\vec{r}, t) \vec{p}(\vec{r}, t)$ is spin diffusion, which is an overall spin-conserving process. Other, spin non-conserving, processes are much slower in ultra cold Fermi gas experiments and are neglected hereafter. The gradient of the non-equilibrium magnetization $\nabla \vec{M} = \vec{p} \nabla M + M \nabla \vec{p}$ drives two distinct spin currents¹⁶: The first term produces a longitudinal spin current parallel to \vec{M} and the second term induces a transverse spin current orthogonal to \vec{M} . These spin currents are proportional

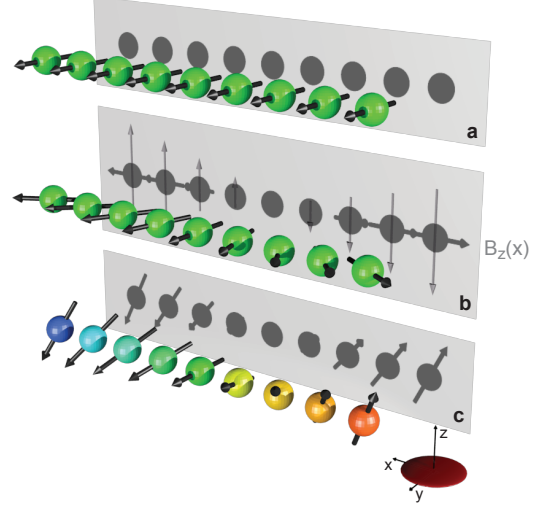


FIG. 1. Quench of a two-dimensional Fermi gas in which all atoms were initially prepared in the $|\downarrow\rangle$ state. (a), A $\pi/2$ -pulse prepares the Fermi gas polarized in the S_y -direction. (b) A magnetic field gradient $\partial B_z/\partial x$ causes the spins to acquire different phase-angles $\phi(x)$ in the equatorial plane. (c) Collisions cant the spins out of the equatorial plane due to the identical spin rotation effect. The acquired projection along S_z together with the motion of the atoms in the harmonic trap impedes rephasing of the spins when the magnetic field gradient is reversed. The spin states are illustrated in the rotating frame.

to the longitudinal \mathcal{D}_{\parallel} and transverse spin diffusivity \mathcal{D}_{\perp} , respectively.

In general, the spin diffusivity in D dimensions behaves as $\mathcal{D} = v l_{\text{mfp}}/D$, where v is the collision velocity and l_{mfp} is the mean free path. The mean-free path is determined by the elastic scattering cross section σ between atoms. For short-range s-wave interactions at unitarity, the cross section attains its maximum value allowed by quantum mechanics $\sigma \sim 1/\lambda_{dB}^{D-1}$, where λ_{dB} is the de-Broglie wavelength of the colliding particles. At high temperatures in the classical gas regime, the spin diffusion constant hence scales as $\mathcal{D} \propto T^{D/2}$ (up to logarithmic corrections in two dimensions owing to the energy dependence of the cross-section¹⁰). In the degenerate regime (of any dimensionality), the situation is quite different: the de-Broglie wavelength λ_{dB} is of order $1/k_F$ and hence the mean-free path is $l_{\text{mfp}} = 1/(n\sigma) \approx 1/k_F$, where k_F is the Fermi wave vector of the gas and $n \sim k_F^D$ is the density. Hence, the spin diffusion constant is given by Planck's constant \hbar divided by the mass m of the particle carrying the spin. This quantum limit can also be viewed

as a result of the uncertainty principle by noticing that the mean-free path is limited by the mean interparticle spacing¹¹. The simple scaling argument, however, hides much of the rich underlying physics. In particular, it cannot explain the Leggett-Rice effect^{13,14,17}, the difference between longitudinal and transverse spin diffusivities¹⁸, and the transition to weak interactions where the physics changes because the system evolves from hydrodynamic to collisionless. So far, lowest spin diffusion constant has been measured for longitudinal spin currents to be $\mathcal{D}_{\parallel} = 6.3\hbar/m$ in three-dimensional degenerate Fermi gases at unitarity⁵, approximately two orders of magnitude smaller than in semiconductor nanostructures¹⁵.

Here, we study the coherence properties of a transversely polarized two-dimensional Fermi gas under the influence of magnetic field gradient. By employing the spin-echo technique¹² we gain access to the intriguing, but little understood, transverse spin dynamics in two-dimensional Fermi systems¹⁶. The experiment starts with a polarised Fermi gas, where all spins are in the same state $|\downarrow\rangle$. Three resonant rf-pulses are applied to rotate the spin state by respective angles $\pi/2 - \pi - \pi/2$ about a fixed axis in spin space, S_x . Consecutive pulses are separated by a time τ and we refer to the spin evolution time as $t = 2\tau$. The initial $\pi/2$ -pulse creates transverse spin polarisation in a coherent superposition between $|\downarrow\rangle$ and $|\uparrow\rangle$ (see Fig. 1a). An applied magnetic field gradient $B' \equiv \partial B_z / \partial x$ gives rise to a transverse spin wave (see Figure 1b) of wave vector $Q = \delta\gamma t B'$, where $\delta\gamma = 152 \text{ kHz/G}$ is the differential gyromagnetic ratio between $|\uparrow\rangle$ and $|\downarrow\rangle$ at 209 G and t is the evolution time (see Methods). On time scales much shorter than the trapping period, Q is independent of the interaction strength¹⁹, and nearby atoms acquire a relative phase-angle of $\Delta\phi \approx Q/k_F$. This lifts the spin-polarisation of the Fermi gas and the spins can collide with each other as they move in the harmonic potential or diffuse. Trivial dephasing induced by the magnetic field gradient is reversed by the π -pulse and the spin state refocus after a time τ if no decoherence has occurred. The final $\pi/2$ -pulse maps the spin state from the S_y onto S_z , which is measured by performing a Stern-Gerlach experiment in time of flight, and we record $\langle M_z \rangle = (N_{\uparrow} - N_{\downarrow}) / (N_{\uparrow} + N_{\downarrow})$.

Even though the interaction potential between atoms is not explicitly spin-dependent, an effective spin-exchange interaction is mediated by the required antisymmetrisation of the scattering wave function. In binary collisions, this leads to the identical spin rotation effect²⁰: in a collision both spins rotate about the axis defined by the sum of their spin orientations. In the Fermi degenerate regime, the binary collision picture has to be replaced by Landau's quasiparticle description. Here, quasiparticle excitations can be considered being affected by a ‘‘molecular field’’ resulting from the effective spin-exchange interaction^{13,14,21,22}. As a result, the spin wave cants out of the $S_x - S_y$ -plane and forms a spin spiral which acquires a component along S_z (see Figure 1c). The magnitude of the identical spin rota-

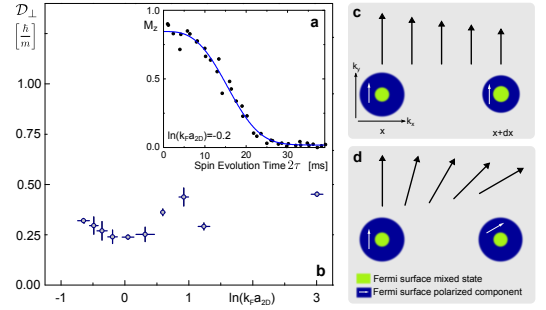


FIG. 2. Spin-echo signals in the strongly interacting regime. **a**, Spin echo-signal at $\ln(k_F a_{2D}) = -0.2$. The blue line is a fit $\propto \exp[-(2\Gamma\tau)^3]$. **b**, Transverse spin diffusion constant \mathcal{D}_{\perp} as a function of interaction strength deduced from the decay constant Γ of the spin-echo signal. Illustration of the different spatial variation of Fermi surfaces of a polarized Fermi gas for the case of longitudinal (c) and transverse (d) spin diffusion.

tion effect is proportional to the mean-field interaction strength $g = -2\pi\hbar^2/[m \ln(k_F a_{2D})]$ of the gas. Here, k_F is the Fermi wave vector for the initially spin-polarized sample, and a_{2D} is the two-dimensional scattering length, which is linked to the binding energy of the confinement-induced dimer by²³ $E_B = \hbar^2/m a_{2D}^2$.

In the strongly interacting regime, i.e., $-1 < \ln(k_F a_{2D}) < 3$, spin transport is dominated by diffusion and the spin-echo signal attains a characteristic non-exponential decay of the form^{12–14} $\propto \exp[-(2\Gamma\tau)^3]$. Fitting the envelope of the spin-echo signal²⁴ (see Figure 2a) with this function we deduce the transverse spin diffusion constant from the measured decay rate as^{12,25} $\mathcal{D}_{\perp} = 12\hbar^2\Gamma^3/(\delta\gamma B')^2$. We extract the transverse spin diffusion constant for various interaction strengths and find $\mathcal{D}_{\perp} = 0.25(3)\hbar/m$ at a shallow minimum around $\ln(k_F a_{2D}) = 0$ (see Figure 2b). From the arguments given at the beginning, we expect the diffusivity to be on the order of \hbar/m . Observing a smaller value than for longitudinal spin diffusion in three dimensions⁵ is probably less linked to the dimensionality rather than to the phase space available for collisions necessary to drive spin diffusion¹⁸: In the case of longitudinal spin currents, a gradient of the $M_z(x)$ polarization along the x-direction can be considered as a spatial variation of the local Fermi surfaces $k_{F,\uparrow}(x)$ and $k_{F,\downarrow}(x)$ (see Fig. 2c). Only $|\uparrow\rangle$ spins in a small region near the Fermi surface can diffuse from x to $x+dx$, invoking the typical T^{-2} scaling for quasiparticles in the deeply degenerate regime. In contrast, in the case of transverse spin currents the Fermi surfaces at different positions are of the same size but have slightly different directions of magnetization. (see Fig. 2d). Hence, a spin moving along x from anywhere between the Fermi surfaces for spin-up and down must scatter to reach local equilibrium, which scales as $n_{\uparrow} - n_{\downarrow}$ and provides a much larger phase space. The result is that for a degenerate system the transverse diffusivity is smaller than the longitudinal and becomes independent of temperature¹⁸.

For a repulsively interacting Fermi gas in three dimen-

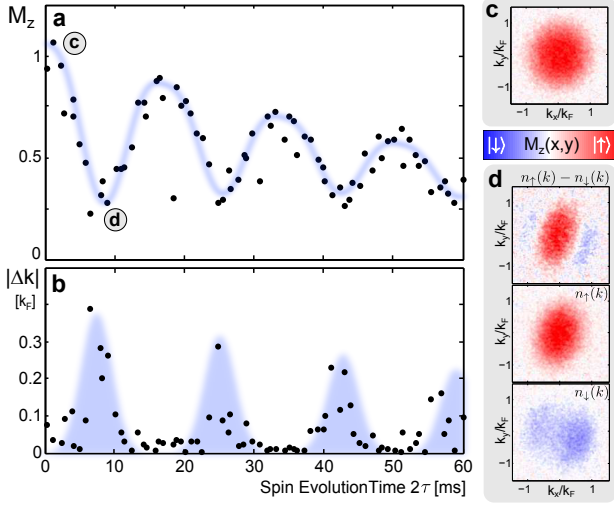


FIG. 3. Observation of spin wave for the non-interacting gas, i.e., $\ln(k_F a_{2D}) \rightarrow +\infty$: **a**, We plot the envelope of the spin-echo signal (dots) and show the fit function (grey line). **b**, centre of mass separation of $|\uparrow\rangle$ and $|\downarrow\rangle$ after 11.8 ms of time of flight. **c** and **d**, momentum distribution of local spin polarisation for large and small spin polarisation, respectively. The lower two panels in **d** show the distribution of spin up and down, respectively.

sions the decay of a spin-spiral state into a Stoner itinerant ferromagnet was considered¹⁹. In this case, the growth rate of the instability towards the formation of the ferromagnet order was found to scale $\propto Q^2$ and hence the spin-polarisation signal would decay $\propto \exp[-(\alpha t)^3]$, similar to spin diffusion.

In the weakly interacting attractive Fermi liquid regime²⁶, i.e., $\ln(k_F a_{2D}) > 3$, we observe a qualitatively different behaviour (see Figure 3a). The envelope of the spin-echo signal decays exponentially and is modulated by a slow oscillation and both the frequency and the damping constant of the oscillation depend on the interaction strength. We attribute this slow periodic modulation to transverse spin waves which are excited by the spin-echo sequence. The spin current induced by the magnetic field gradient can only be inverted completely by the π -pulse when applied in phase with the harmonic motion. This can be qualitatively (for zero interactions) understood in a phase-space picture by considering that the magnetic field gradient causes a spatial offset between the potentials for the $|\uparrow\rangle$ and the $|\downarrow\rangle$ spin states and, correspondingly, the phase-space trajectories of the two spin-components are displaced⁹. Indeed, we observe that the difference of the center-of-mass momenta $\langle k_\uparrow \rangle - \langle k_\downarrow \rangle$ of the two spin densities $n_\uparrow(k)$ and $n_\downarrow(k)$ oscillates out-of-phase with the contrast of the spin-echo signal (Figure 3a and 3e). The total density profile $n(k) = n_\uparrow(k) + n_\downarrow(k)$ is stationary, which indicates a pure spin mode.

The measured envelope of the spin-echo signal (see Fig. 3a) is fitted with an empirical function of the form: $A \exp(-\gamma t) (1 - B |\sin(\omega t/2)|^3) + C$. Here, $|A|, |B| \sim$

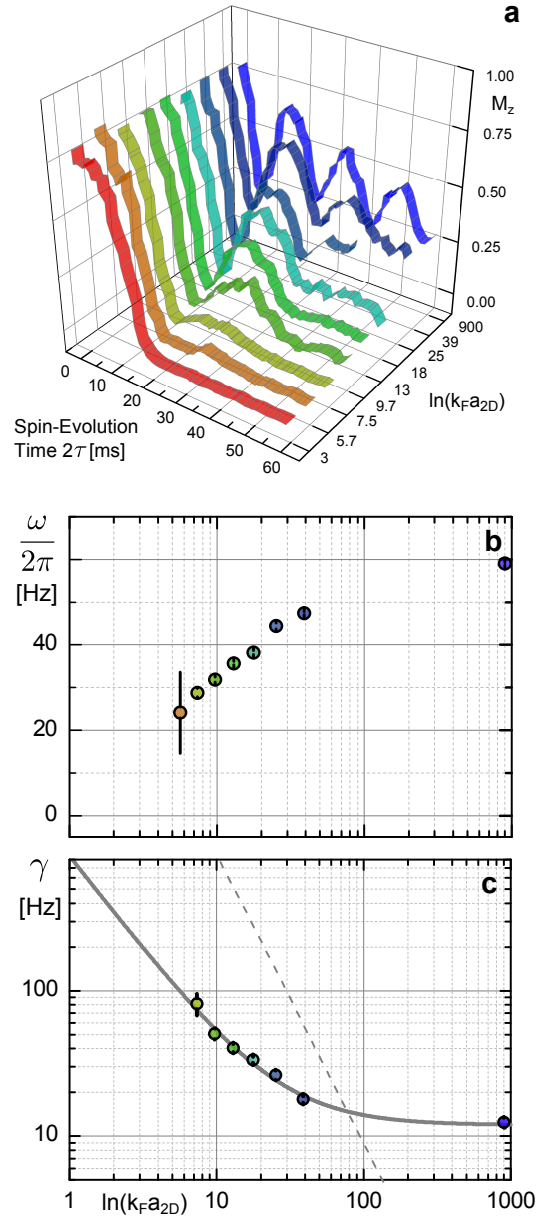


FIG. 4. Spin wave in the collisionless regime as function of interaction strength. **a**, Time evolution of global spin polarization for different interaction strengths. **b**, Frequency of oscillating spin-polarization. For the data point at $\ln(k_F a_{2D}) = 3$ we were not able to fit a frequency and set the value to zero. **c** Damping coefficient γ of the spin-polarization. The dashed line indicates the elastic scattering rate and the solid line is a fit to the measured decay.

$\mathcal{O}(1)$ and $|C| \ll 1$ are amplitudes and a global offset of the spin echo signal, respectively. We find that this periodic function of frequency ω is approximating the non-sinusoidal signal best. The exponent is fixed to the value 3 for all interactions, and we do not see a large influence on the deduced parameters. Both the frequency ω and the exponential damping γ depend on the interaction strength of the gas.

For zero interaction strength the mode is at half the trap frequency and we observe a softening of the spin mode when approaching the hydrodynamic regime (Figure 4a and b). Such a behaviour is reminiscent of the collisionless-to-hydrodynamic transition of the spin-dipole oscillation^{5,27}, whereas spin-symmetric modes have non-zero frequencies even in the hydrodynamic regime²⁸. The decay rate γ of the oscillation (see Figure 4c) is found smallest for the non-interacting gas, where it is two orders of magnitude smaller than the dephasing rate $1/\tau_{\text{Ramsey}}$ in the inhomogeneous magnetic field (see Methods). As the interaction strength is increased, the rate γ is growing (see Fig. 4c). We fit this growth with a power-law behaviour $\gamma = \alpha/\ln(k_F a_{2D})^\beta + \gamma_0$ and we determine the exponent to be $\beta = 1.3 \pm 0.15$. Observing a scaling with an exponent close to unity signals that the loss of global coherence is dominated by the identical spin-rotation effect, which scales proportional to the mean-field interaction strength g . In contrast, the rate of elastic collisions scales as $\propto 1/\ln(k_F a_{2D})^2$, i.e., $\beta = 2$ (see dashed line in Fig. 4c). This suggests the following decoherence mechanism in a spin-1/2 Fermi gas: after building up in the magnetic field gradient, the spin wave decays when neighbouring atoms have acquired a sufficiently large phase-angle $\Delta\phi$ between their spins such that in a spin-conserving collision both spins rotate out of the $S_x - S_y$ -plane. Initially, this is a coherent process, which subsequently dephases due to the coupling of the spin-rotation to the momentum of the atoms²⁹. This picture contrasts to the previously conjectured mechanism of the decoherence of a spin mixture resulting from a magnetic field curvature^{3,30}, which has been probed, for example, using the Ramsey technique³⁰. Our spin-echo measurements show that the dephasing time measured by the Ramsey technique underestimates than the actual spin decoherence time in the weakly interacting regime by orders of magnitude, affecting the question of the equilibration of the Fermi gas.

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I. METHODS

A. Preparation of the two-dimensional gases

We prepare a quantum degenerate Fermi gas of ⁴⁰K atoms in a one-dimensional optical lattice of wavelength

$\lambda = 1064\text{ nm}$ populating a stack of approximately 40 individual two-dimensional quantum gases^{31,32}. The radial confinement of the two-dimensional gases is harmonic with a trap frequency of $\omega_r = 2\pi \times 127\text{ Hz}$ and the axial trap frequency is $\omega_z = 2\pi \times 75\text{ kHz}$. Using a radio-frequency cleaning pulse, we ensure preparation of a spin-polarized gas in the $|F = 9/2, m_F = -9/2\rangle \equiv |\downarrow\rangle$ ground state with 1.5×10^5 atoms, corresponding to the Fermi energy of the spin-polarised gas $E_F = 12.3(2.0)\text{ kHz}$ at a temperature of $k_B T/E_F = 0.24(3)$. The coupling strength of a two-dimensional Fermi gas is given by the parameter $g = -2\pi\hbar^2/[m \ln(k_F a_{2D})]^{23}$. Here, k_F is the Fermi wave vector for the initially spin-polarized sample, and a_{2D} is the two-dimensional scattering length which is linked to the binding energy of the confinement-induced dimer by $E_B = \hbar^2/ma_{2D}^2$.

Our experiments on the spin dynamics start by ramping the magnetic field from $B = 209.15\text{ G}$ to the desired value B near the Feshbach resonance in 30 ms and wait for 200 ms. Subsequently we apply the spin-echo pulse sequence (see main text) of three radio-frequency pulses with frequencies of $\sim 50\text{ MHz}$. The pulses have a square envelope and duration of $t_{\pi/2} \sim 46\text{ }\mu\text{s}$ for a $\pi/2$ -pulse and $2 \times t_{\pi/2}$ for a π -pulse. The pulses are separated by the same time τ which gives the total spin evolutions time $t = 2\tau$.

B. Ramsey measurements: Dephasing in the magnetic field gradient

We assess the time scale of simple dephasing of the spin in the magnetic field gradient by performing Ramsey spectroscopy on the non-interacting gas using the following sequence: the initial $\pi/2$ -pulse is followed by a second $\pi/2$ -pulse with a variable time delay τ . We observe a Ramsey coherence time of $\tau_{\text{Ramsey}} = (600 \pm 30)\text{ }\mu\text{s}$. Since the Ramsey time is more than an order of magnitude shorter than the inverse trap frequency, we neglect the motional contribution to the dephasing. Instead, we relate the Ramsey time to the dephasing time of the (quasi stationary) spins across the whole cloud, and we find from this the magnetic field gradient. We fit the data with $P(t) = \frac{8NJ_2(\phi)}{\phi^2}$ Where, $\phi = 2\pi\Delta t = d\gamma B' R_F t$. Δ is the Zeeman shift due to the gradient at the edge of the cloud compared to the center. The fit function fits $\phi = bt$, i.e., $b = 2\pi\Delta$. The fit results gives $b = 8.1(1)\text{ kHz}$ and we know $d\gamma = 152\text{ kHz/G}$ at 209.15 G and $R_F = 17.7\text{ }\mu\text{m}$.

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